

## Geometry

## Chapter 3 Review Parallel &amp; Perpendicular Lines

Name Key

Block \_\_\_\_\_

Date \_\_\_\_\_

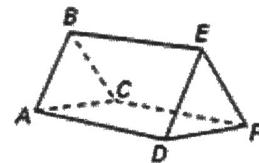
Think of each segment in the diagram as part of a line. Fill in the blank with *parallel*, *skew*, or *perpendicular*.

1.  $\overline{DE}$  and  $\overline{CF}$  are skew.

2.  $\overline{AD}$ ,  $\overline{BE}$ , and  $\overline{CF}$  are parallel.

3. Plane ABC and plane DEF are parallel.

4.  $\overline{BE}$  and  $\overline{AB}$  are perpendicular.



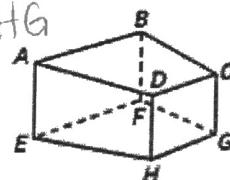
3-1 Think of each segment in the diagram as part of a line. There may be more than one right answer.

5. Name a line perpendicular to  $\overline{HD}$ .  $\overline{DC}$  or  $\overline{DA}$  or  $\overline{HE}$  or  $\overline{HG}$

6. Name a plane parallel to DCH.  $\square ABCF$

7. Name a line parallel to  $\overline{BC}$ .  $\overline{DG}$

8. Name a line skew to  $\overline{FG}$ .  $\overline{AE}$  or  $\overline{AB}$  or  $\overline{DH}$  or  $\overline{DC}$



3-2 Complete the statement with *corresponding*, *alternate interior*, *alternate exterior*, or *consecutive interior*.

9.  $\angle 4$  and  $\angle 8$  are alt. int. angles.

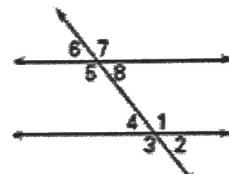
10.  $\angle 2$  and  $\angle 6$  are alt. ext. angles.

11.  $\angle 1$  and  $\angle 8$  are same-side int. angles.

12.  $\angle 7$  and  $\angle 2$  are none N/A angles.

13.  $\angle 4$  and  $\angle 5$  are same-side int. angles.

14.  $\angle 5$  and  $\angle 1$  are alt. int. angles.



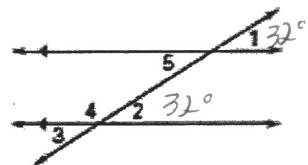
3-3 16. Given that  $m\angle 1 = 32^\circ$ , find each measure. Tell which postulate or theorem you use.

a.  $m\angle 2$   $32^\circ$  corresponding with  $\angle 1$

b.  $m\angle 3$   $32^\circ$  vertical with  $\angle 2$

c.  $m\angle 4$   $148^\circ$  linear pair with  $\angle 2$

d.  $m\angle 5$   $32^\circ$  vertical with  $\angle 1$



3-2 17. Use properties of parallel lines to find the value of  $x$ .

$$\begin{aligned} a. \quad (9x + 7)^\circ & \quad 115^\circ \\ 9x + 7 &= 115 \\ -7 &\quad -7 \\ 9x &= 108 \\ \frac{9}{9} &\quad \boxed{x = 12} \end{aligned}$$

$$\begin{aligned} b. \quad 4x - 3 + 135 &= 180 \\ 4x + 132 &= 180 \\ -132 &\quad -132 \\ 4x &= 48 \\ \frac{4}{4} &\quad \boxed{x = 12} \end{aligned}$$

$$\begin{aligned} c. \quad 14x + 7 + 103 &= 180 \\ 14x + 110 &= 180 \\ -110 &\quad -110 \\ 14x &= 70 \\ \frac{14}{14} &\quad \boxed{x = 5} \end{aligned}$$

$$\begin{aligned} d. \quad 14x + 7 + 103 &= 180 \\ 14x + 110 &= 180 \\ -110 &\quad -110 \\ 14x &= 70 \\ \frac{14}{14} &\quad \boxed{x = 5} \\ 2x + 4 &= 140 \\ -4 &\quad -4 \\ 2x &= 136 \\ \frac{2}{2} &\quad \boxed{x = 68} \end{aligned}$$

3-3 18. Prove the statement from the given information.

a. Prove:  $l \parallel m$

$$\begin{aligned} l & \quad m \\ 120^\circ & \quad 60^\circ \\ 120^\circ & \quad \boxed{1} \\ \angle 1 + \angle 6 &= 180^\circ \\ \text{b/c linear pair} & \\ \angle 1 &\cong 120^\circ \\ \text{alt. ext. } \angle \text{ converse} & \end{aligned}$$

b. Prove:  $n \parallel o$

$$\begin{aligned} l & \quad m \\ 135^\circ & \quad 135^\circ \\ 45^\circ & \quad \boxed{2} \\ 135^\circ + 45^\circ &= 180^\circ \\ \text{b/c vertical } \angle's & \\ \text{Same-side int. } \angle \text{ converse} & \end{aligned}$$

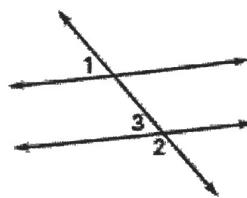
$$\begin{aligned} 3-4 \quad n & \quad o \\ 6x &= 90 \\ \frac{6}{6} &\quad \boxed{x = 15} \\ (6x) & \quad (5x) \end{aligned}$$

$$\begin{aligned} l & \quad m \\ 120^\circ & \quad 60^\circ \\ 120^\circ & \quad \boxed{1} \\ \angle 1 + \angle 6 &= 180^\circ \\ \text{b/c linear pair} & \\ \angle 1 &\cong 120^\circ \\ \text{alt. ext. } \angle \text{ converse} & \end{aligned}$$

- 20) Complete the following proof by providing the reasons.

Given:  $m\angle 1 = 53^\circ$   
 $m\angle 2 = 127^\circ$

Prove:  $j \parallel k$



Statements

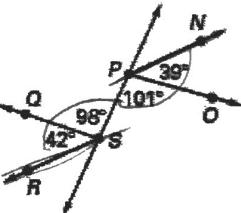
1.  $m\angle 1 = 53^\circ$   
 $m\angle 2 = 127^\circ$
2.  $m\angle 3 + m\angle 2 = 180$
3.  $m\angle 3 + 127 = 180$   
 $\cancel{-127} \quad \cancel{-127}$
4.  $m\angle 3 = 53$
5.  $m\angle 3 = m\angle 1$
6.  $\angle 3 \cong \angle 1$
7.  $j \parallel k$

Reasons

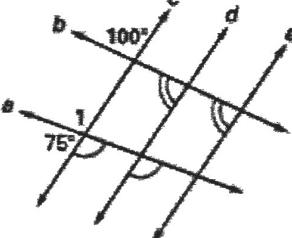
1. Given
2. Linear pair postulate
3. Substitution prop.
4. Subtraction prop.
5. Substitution prop.
6. def. of congruent
7. corresponding  $\angle$  converse

21. Determine which rays are parallel.

- a. Is  $\overrightarrow{PN}$  parallel to  $\overrightarrow{SR}$ ? yes  $140^\circ = 140^\circ \checkmark$   
b. Is  $\overrightarrow{PO}$  parallel to  $\overrightarrow{SQ}$ ? no!,  $98^\circ \neq 101^\circ \times$

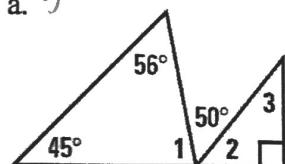


22. Determine which lines, if any must be parallel.



$$\begin{aligned} d &\parallel e \\ c &\parallel d \\ e &\parallel c \end{aligned}$$

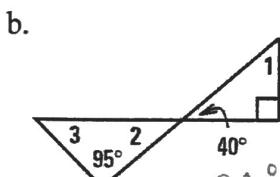
23. In the triangles below, find the missing angles.



$$\angle 1 = 79^\circ$$

$$\angle 2 = 51^\circ$$

$$\angle 3 = 39^\circ$$



$$\angle 1 = 50^\circ$$

$$\angle 2 = 40^\circ$$

$$\angle 3 = 45^\circ$$

c.

$$\begin{aligned} 5(x) &= 95^\circ \\ 5x &= 95 \\ x &= 19 \end{aligned}$$

$$\begin{aligned} 2(x+5) &= 130^\circ \\ 2(19+5) &= 130 \\ 48 &= 130 \end{aligned}$$

$$5x + 2x + 5 + 3x - 15 = 180$$

$$\begin{aligned} 10x - 10 &= 180 \\ +10 &+10 \\ 10x &= 190 \\ \frac{10x}{10} &= \frac{190}{10} \\ x &= 19 \end{aligned}$$

d.

$$\begin{aligned} 38^\circ &= 71^\circ \\ 7x+1 &= 71 \\ 7x &= 70 \\ \frac{7x}{7} &= \frac{70}{7} \\ x &= 10 \end{aligned}$$

$$\begin{aligned} 10(x+9) &= 109^\circ \\ 10(10+9) &= 109 \\ 190 &= 109 \end{aligned}$$

$$10x + 9 = 7x + 1 + 38$$

$$10x + 9 = 7x + 39$$

$$-7x \quad -7x$$

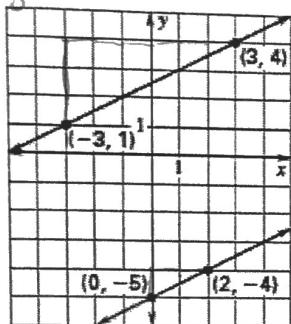
$$3x + 9 = 39$$

$$-9 \quad -9$$

$$\frac{3x}{3} = \frac{30}{3}$$

$$x = 10$$

- 24) Find the slope of each line. Are the lines parallel?



$$\rightarrow m = \frac{3}{6} = \frac{1}{2}$$

$$\rightarrow m = \frac{1}{2}$$

yes ; the slopes are the same !

- 25) Write an equation of the line that passes through the given point  $P$  and is parallel to the line with the given equation.

a.  $P(10, 3)$ ,  $y = x - 12$

$$m=1 \parallel \leftarrow m=1$$

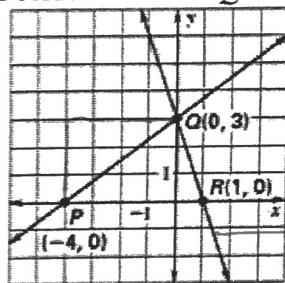
$$y - y_1 = m(x - x_1)$$

$$y - 3 = 1(x - 10)$$

$$y - 3 = x - 10$$

$$y = x - 7$$

- 26) Decide whether  $\overline{PQ}$  and  $\overline{QR}$  are perpendicular.



$$m = \frac{3}{4}$$

$$m = -\frac{3}{1}$$

no

- 28) Line  $j$  is perpendicular to the line with the given equation and line  $j$  passes through  $P$ . Write an equation of line  $j$ .

a.  $7y = -4x + 13$ ,  $P(-2, 6)$

$$m = -\frac{4}{7} \rightarrow \perp \left( m = \frac{7}{4} \right)$$

$$y - y_1 = m(x - x_1)$$

$$y - 6 = \frac{7}{4}(x + 2)$$

$$y - 6 = \frac{7}{4}x + \frac{14}{4}$$

$$y - 6 = \frac{7}{4}x + \frac{14}{4}$$

$$(y = \frac{7}{4}x + \frac{38}{4} \text{ or } y = \frac{7}{4}x + \frac{17}{2})$$

- 29) In the figure,  $\angle 5$  is complementary to  $\angle 12$ , and  $m\angle 9 = 148^\circ$ . Find the measure of each numbered angle in the figure.

$$m\angle 5 = 58^\circ$$

$$m\angle 8 = 122^\circ$$

$$m\angle 11 = 148^\circ$$

$$m\angle 6 = 122^\circ$$

$$m\angle 9 = 148^\circ$$

$$m\angle 12 = 32^\circ$$

b.  $y = -\frac{1}{5}x + \frac{6}{5}$ ,  $P(-1, 2)$

$$m = -\frac{1}{5} \rightarrow \perp \left( m = \frac{5}{1} \right)$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 5(x + 1)$$

$$y - 2 = 5x + 5$$

$$+2 \quad +2$$

$$y = 5x + 7$$

$$y - y_1 = m(x - x_1)$$

$$y - 2 = 5(x + 1)$$

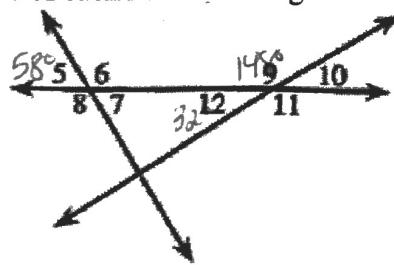
$$y - 2 = 5x + 5$$

$$+2 \quad +2$$

$$y = 5x + 7$$

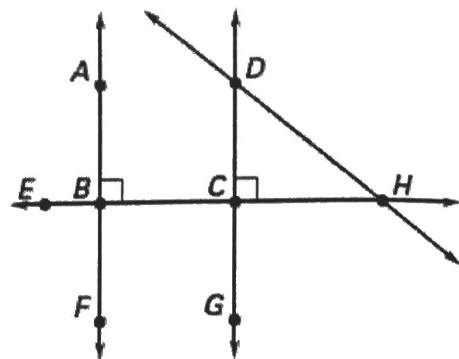
$$m\angle 7 = 58^\circ$$

$$m\angle 10 = 32^\circ$$



Use the figure to determine whether each statement is *true* or *false*.

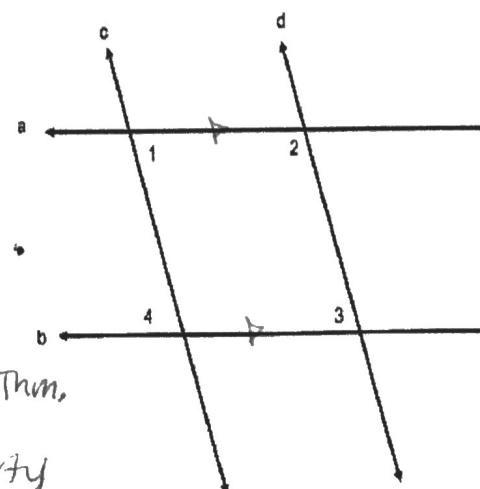
- 30)  $\angle DCB$  and  $\angle DCH$  are supplementary. True
- 31)  $\overline{DH} \perp \overline{EH}$  False
- 32)  $\overline{HE} \perp \overline{AF}$  True
- 33)  $\angle DCB$  and  $\angle ABC$  are complementary. False



34) Given:  $a \parallel b$ ,  $c \parallel d$

Prove:  $\angle 1 \cong \angle 3$

<u>Statements</u>	<u>Reasons</u>
1. $a \parallel b$	1. given
2. $\angle 1 \cong \angle 4$ .	2. alt. int. $\angle$ Thm.
3. $c \parallel d$	3. given
4. $\angle 4 \cong \angle 3$	4. corresponding $\angle$ Thm.
5. $\angle 1 \cong \angle 3$	5. transitive property



35.  $\angle QSR$  and  $\angle UVX$  are supplementary. Complete the proof that  $\overleftrightarrow{RT} \parallel \overleftrightarrow{UW}$ .

<u>Statement</u>	<u>Reason</u>
1 $\angle QSR$ and $\angle UVX$ are supplementary	Given
2 $m\angle QSR + m\angle UVX = 180^\circ$	def. of supplementary
3 $m\angle QSR + m\angle RSV = 180^\circ$	linear pair postulate
4 $m\angle QSR + m\angle UVX = m\angle QSR + m\angle RSV$	substitution prop.
5 $m\angle UVX = m\angle RSV$	subtraction prop.
6 $\overleftrightarrow{RT} \parallel \overleftrightarrow{UW}$	corresponding $\angle$ converse

36. GIVEN:  $g \parallel h$ ,  $\angle 1$  and  $\angle 4$  are supplementary

PROVE:  $p \parallel r$

- Statements
- $g \parallel h$
  - $\angle 1 + \angle 4$  are supplementary
  - $\angle 1 \cong \angle 2$

$$m\angle 2 + m\angle 3 = 180$$

$$m\angle 1 + m\angle 3 = 180$$

$$m\angle 1 + m\angle 4 = 180$$

$$m\angle 3 \cong m\angle 4$$

$$p \parallel r$$

- Reasons
- Given
  - Given
  - alt. int.  $\angle$  Thm.
  - linear pair postulate
  - substitution prop.
  - def. of supplementary
  - congruent supplements
  - alt. int.  $\angle$  converse

